# Algorithms and Data Structures.

# Examination questions.

Year: 2021

#### Organizational issues:

- You need to receive at least 38 pts <u>before</u> the exam to be admitted.
- You need to receive at least 22 pts at the exam to pass it successfully.
- Each question is scored 10, 20 or 30 pts. The score is the maximum score you get for <u>perfect</u> answer.
- Each ticket contains 2 questions that have the total score of 40 pts.

#### General requirements for the answers:

- For questions that consider algorithm, time complexity estimation must be supplied.
- For questions that consider data structure, basic operations time complexity estimation must be supplied.
- For each question you should supply an example that demonstrates definitions and algorithm.

## Module 1. Introduction to algorithms and data structures.

- 1. Insertion sort: algorithm; using array and dynamic list to implement insertion sort. Time and space complexity estimation. {20 pts}
- 2. Graphs: definition; edge list representation. Time complexity of basic operations using edge list representation. {10 pts}
- 3. Graphs: definition; adjacency matrix representation. Time complexity of basic operations using adjacency matrix representation. {10 pts}
- 4. Graphs: definition; adjacency list representation. Time complexity of basic operations using adjacency list representation. {10 pts}
- 5. Depth-first search: recursive implementation; stack-based implementation. {20 pts}
- 6. Stack: abstract data structure; array-based implementation. {10 pts}
- 7. Stack: abstract data structure; linked list-based implementation. {10 pts}
- 8. Queue: abstract data structure; linear array-based implementation. {10 pts}
- 9. Queue: abstract data structure; circular array-based implementation. {10 pts}
- 10. Queue: abstract data structure; linked list-based implementation. {10 pts}
- 11. Breadth-first search: queue-based implementation. {10 pts}
- 12. Connected components detection with DFS or BFS. {10 pts}
- 13. Bipartiteness check algorithm. {10 pts}
- 14. DAGs: definition, topological sort (definition and algorithm). {20 pts}

# Module 2. Greedy algorithms. Divide-and-Conquer strategy.

- 15. Minimum spanning tree: problem definition. {10 pts}
- 16. Kruskal's algorithm: general scheme; (improved) implementation with array-based safety check procedure. {20 pts}
- 17. Kruskal's algorithm: general scheme; implementation with safety check procedure based on reversed trees data structure. {20 pts}
- 18. Prim's algorithm: general scheme; naïve and priority queue-based implementation. {20 pts}
- 19. Priority queue: abstract data structure, unsorted array implementation. {10 pts}
- 20. Priority queue: abstract data structure, sorted array implementation. {10 pts}
- 21. Priority queue: abstract data structure, dynamic linked sorted list implementation. {10 pts}
- 22. Priority queue: abstract data structure, binary search tree implementation. {20 pts}
- 23. Priority queue: abstract data structure, 2-3 tree implementation. {20 pts}
- 24. Binary heap: abstract data structure, complete binary tree implementation. {30 pts}

- 25. Merge sort as a divide-and-conquer algorithm. {20 pts}
- 26. Master theorem for divide-and-conquer algorithms. Proof of the simplified version of Master theorem. {20 pts}
- 27. Integer multiplication: the standard and Karatsuba's algorithms. {20 pts}
- 28. Fast exponentiation algorithm. {10 pts}
- 29. Strassen's algorithm for matrix multiplication. {10 pts}

## Module 3. Dynamic programming.

- 30. A general scheme of a simple version of a dynamic programming algorithm and meta-algorithm for transforming a recursive algorithm into a DP algorithm. Demonstration for Fibonacci numbers calculating. {20 pts}
- 31. Graph distances: definitions, three problem formulations. {10 pts}
- 32. The principle of optimality for graph distances. Troubles with negative weights. {20 pts}
- 33. Dijkstra's algorithm for a general graph without negative cycles. Building a shortest path.
- 34. Dijkstra's algorithm for a graph without negative edges. Building a shortest path.
- 35. Floyd-Warshall's algorithm for the all-t-all distances problem. Building a shortest path.
- 36. Edit distance: general definition, Levenshtein distance, algorithm for calculating. (30 pts)
- 37. Longest common subsequence problem: definition, Needleman-Wunsch algorithm. {20 pts}
- 38. Building an optimal binary search tree: problem definition, recurrence formula, algorithm. {30 pts}

## Module 4. NP-hard problems.

- 39. Travelling salesman problem: definition. {10 pts}
- 40. Metric TSP: definition. {10 pts}
- 41. Brute-force algorithm for TSP. {20 pts}
- 42. Branch-and-bound method: the general scheme. {20 pts}
- 43. Branch-and-bound method for TSP: bound function variants. {10 pts}
- 44. Performance ratio of an approximate algorithm: definition. {10 pts}
- 45. 2-approximate algorithm for Metric TSP. {20 pts}
- 46. Three greedy heuristics for TSP. {20 pts}
- 47. Local search: the general scheme and its features. {20 pts}
- 48. Local search algorithms for TSP. {20 pts}
- 49. Tabu search. {20 pts}
- 50. Randomizations for local search. {10 pts}

#### Recommended sources

- 1. The course section at the Moodle: <a href="http://edu.mmcs.sfedu.ru/course/view.php?id=551">http://edu.mmcs.sfedu.ru/course/view.php?id=551</a>
- 2. Open Data Structures. An open content textbook. URL: http://opendatastructures.org/
- 3. Jeff Erickson. Algorithms. A free electronic version. URL: <a href="http://jeffe.cs.illinois.edu/teaching/algorithms/">http://jeffe.cs.illinois.edu/teaching/algorithms/</a>
- 4. Clifford A. Shaffer. Data Structures & Algorithm Analysis. A free for educational use electronic book. URL: <a href="https://people.cs.vt.edu/~shaffer/Book/">https://people.cs.vt.edu/~shaffer/Book/</a>
- 5. The Computer Science Handbook. A Reference for Data Structures and Algorithms. URL: <a href="https://www.thecshandbook.com/">https://www.thecshandbook.com/</a>
- 6. Lectures Notes on Algorithm Analysis and Computational Complexity (Fourth Edition) Ian Parberry: URL: <a href="http://ianparberry.com/books/free/license.html">http://ianparberry.com/books/free/license.html</a>
- 7. Kleinberg J., Tardos É. Algorithm Design. Pearson Education Inc., 2006.
- 8. Cormen T.H., Leiserson C.E., Rivest R.L., Stein C. Introduction to Algorithms, 3rd ed. The MIT Press 2009.